

Rapid Comparative Quantitative Analysis of Nuclear Fuel Cycles

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Motivation

- Future of nuclear power uncertain
- Abundance of fuel cycle options:
 - Fuel isotope mix?
 - Fuel recycling: Once-Through/Tiered?
 - Reactor type: Fast/Thermal?
 - Reloading: Single/Batch-Mode?
- Question: Which cycle to use?

Project Aims

- Difficult to compare nuclear cycles
- Focus typically on 2-3 cycle comparison
- Use lumped model to quickly simulate large number of disparate cycles
- Primary aim:

‘Establish a framework of metrics allowing direct comparison between different nuclear cycles’

Reactor Model

- First-order lumped transient model
- First developed to model fast ADSRs by David Coates
- Model adapted to run variety of thermal/fast cycles
- Numerically solves differential equation for each of 49 separate fuel isotopes

Metric Overview

- 3 major metric groups:
 - Efficiency/Sustainability
 - Waste Toxicity
 - Proliferation Hardness/Resistance
- Parity
 - Single v. Multi-tier cycles
 - Thermal v. Fast cycles
 - 50,000GWd energy limit
 - Cycles repeated to reach limit

Sustainability

- Can calculate 'potential' of any atom population
- Allows definition of 'cycle efficiency'

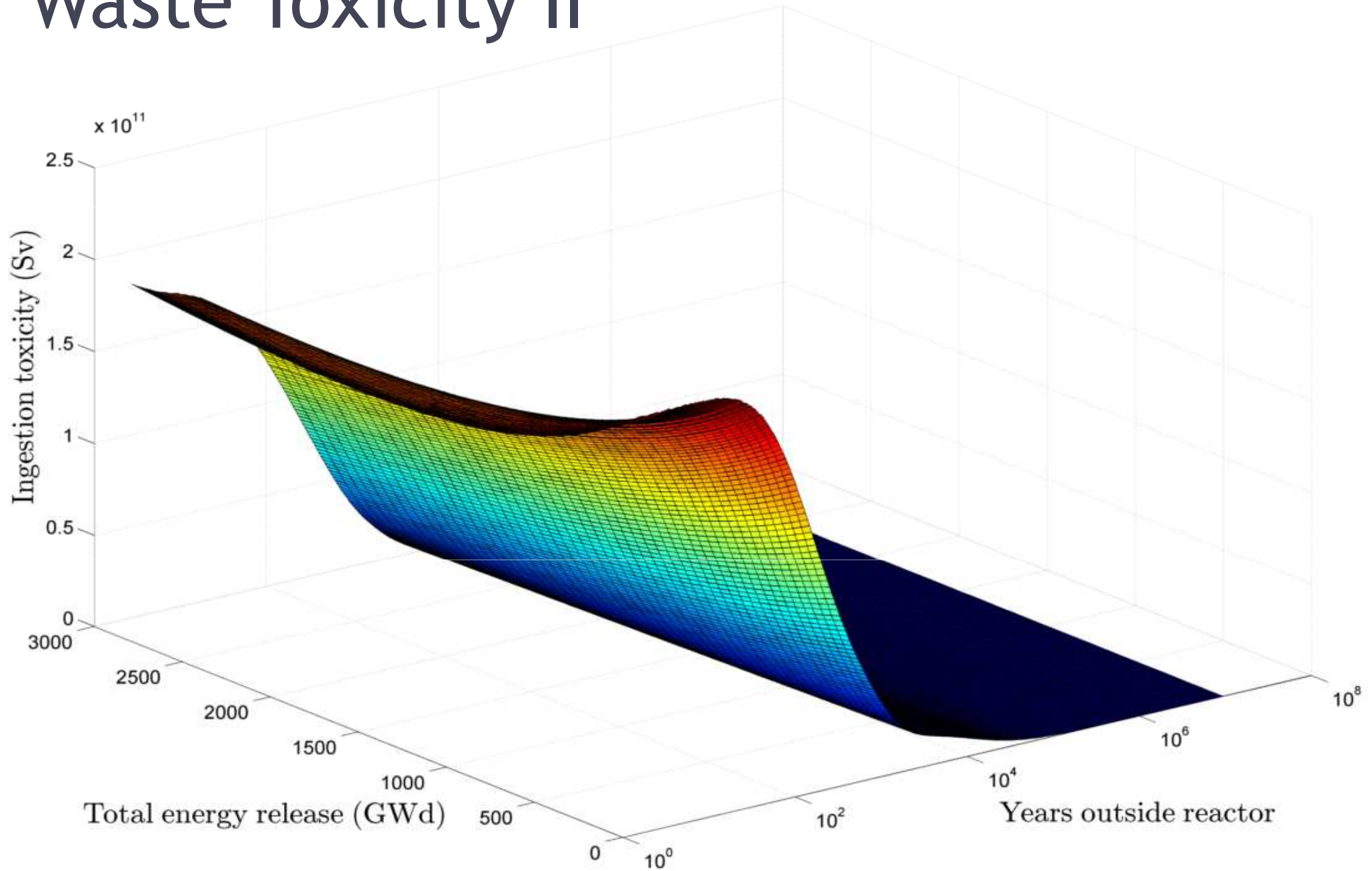
$$\eta_{\text{nuc}} = \frac{\langle \text{Fuel} \rangle - \langle \text{Waste} \rangle}{\langle \text{Fuel} \rangle}$$

- High nuclear efficiency implies cycle extracts high proportion of available energy

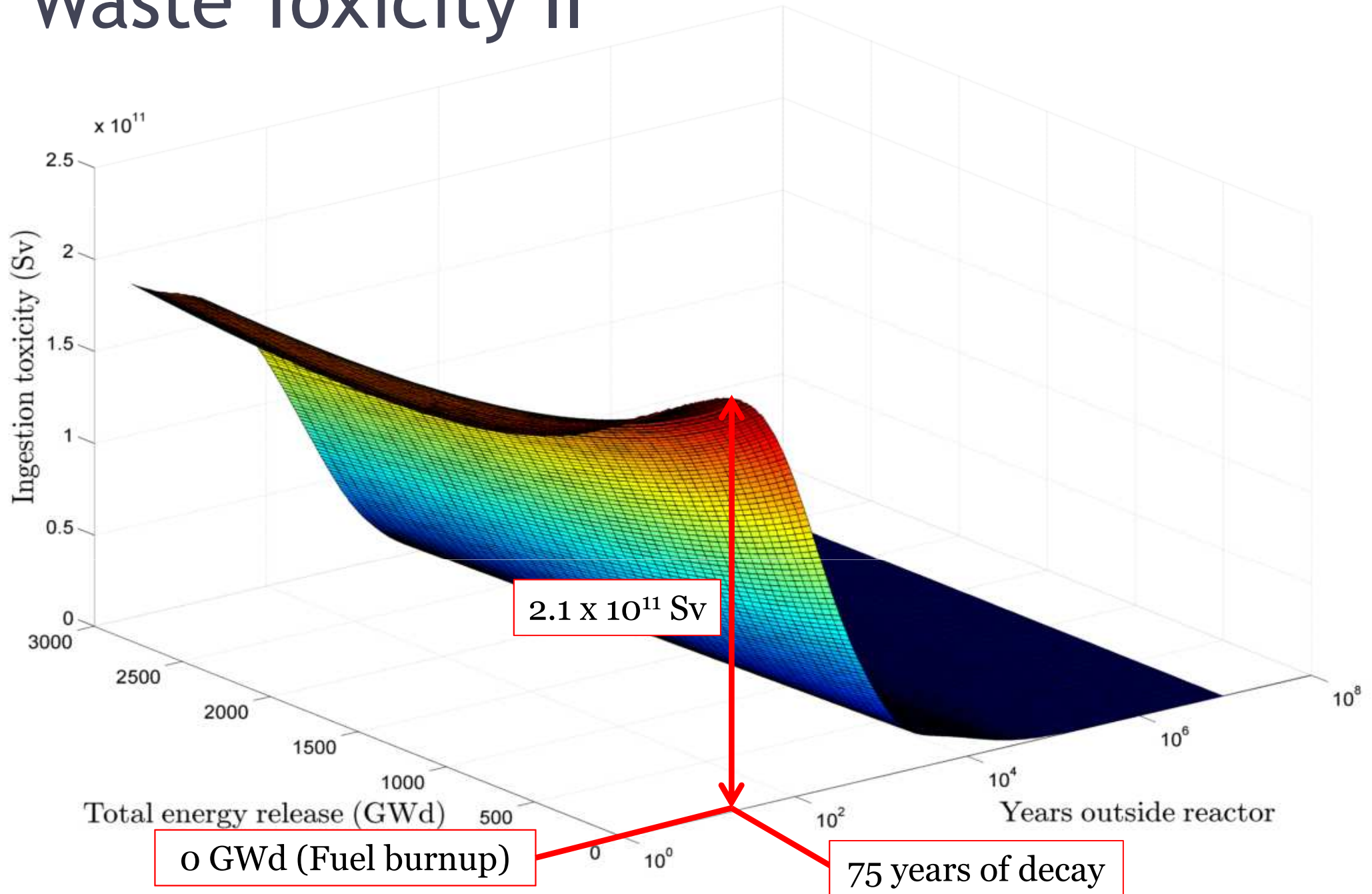
Waste Toxicity I

- Waste composition determined through application of Bateman equations using NEA data
- Ingestive toxicity determined through multiplication by ICRP figures (ICRP 72)
- 9 million year decay period modelled with results verified through comparison to NEA code results

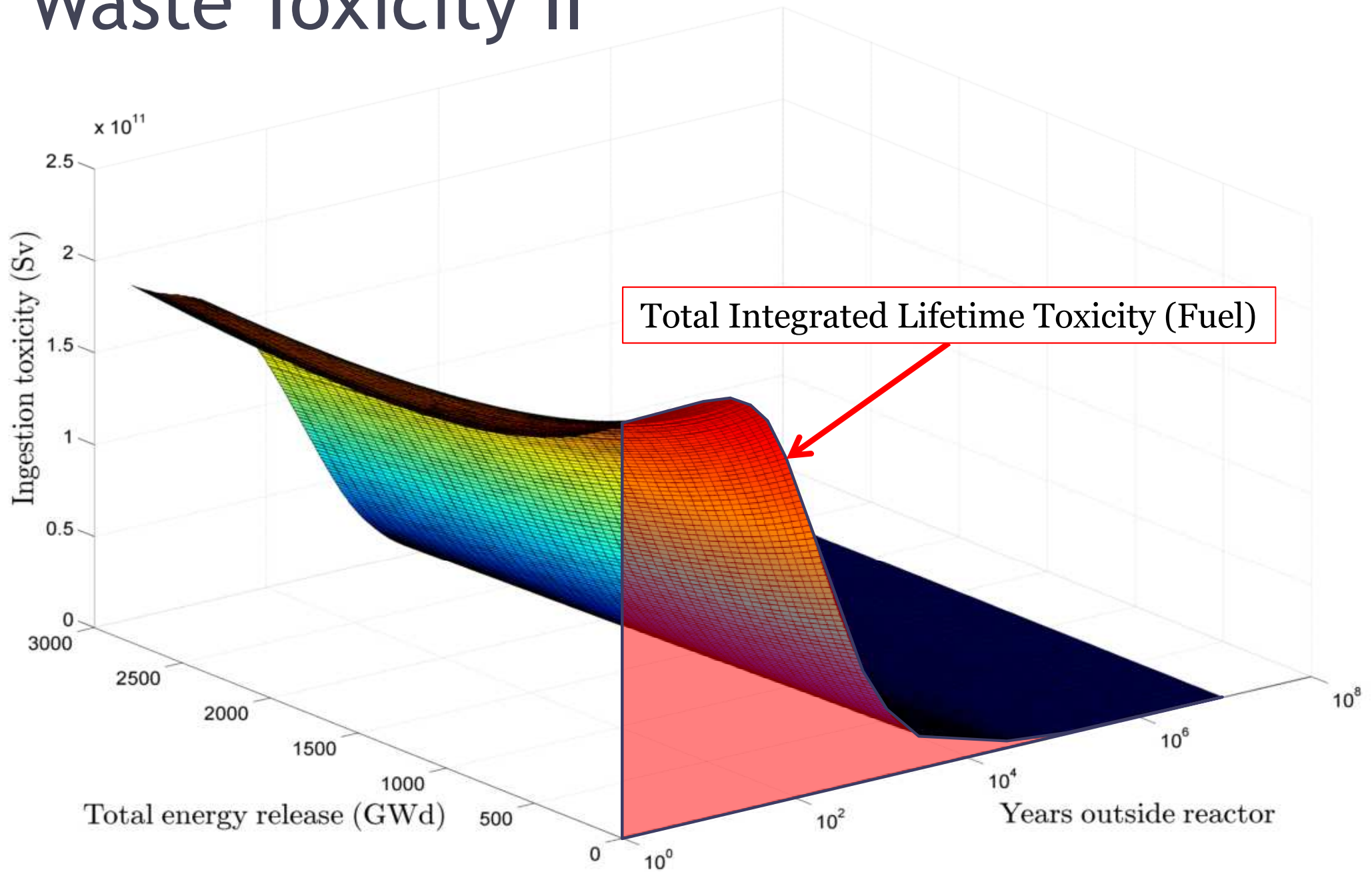
Waste Toxicity II



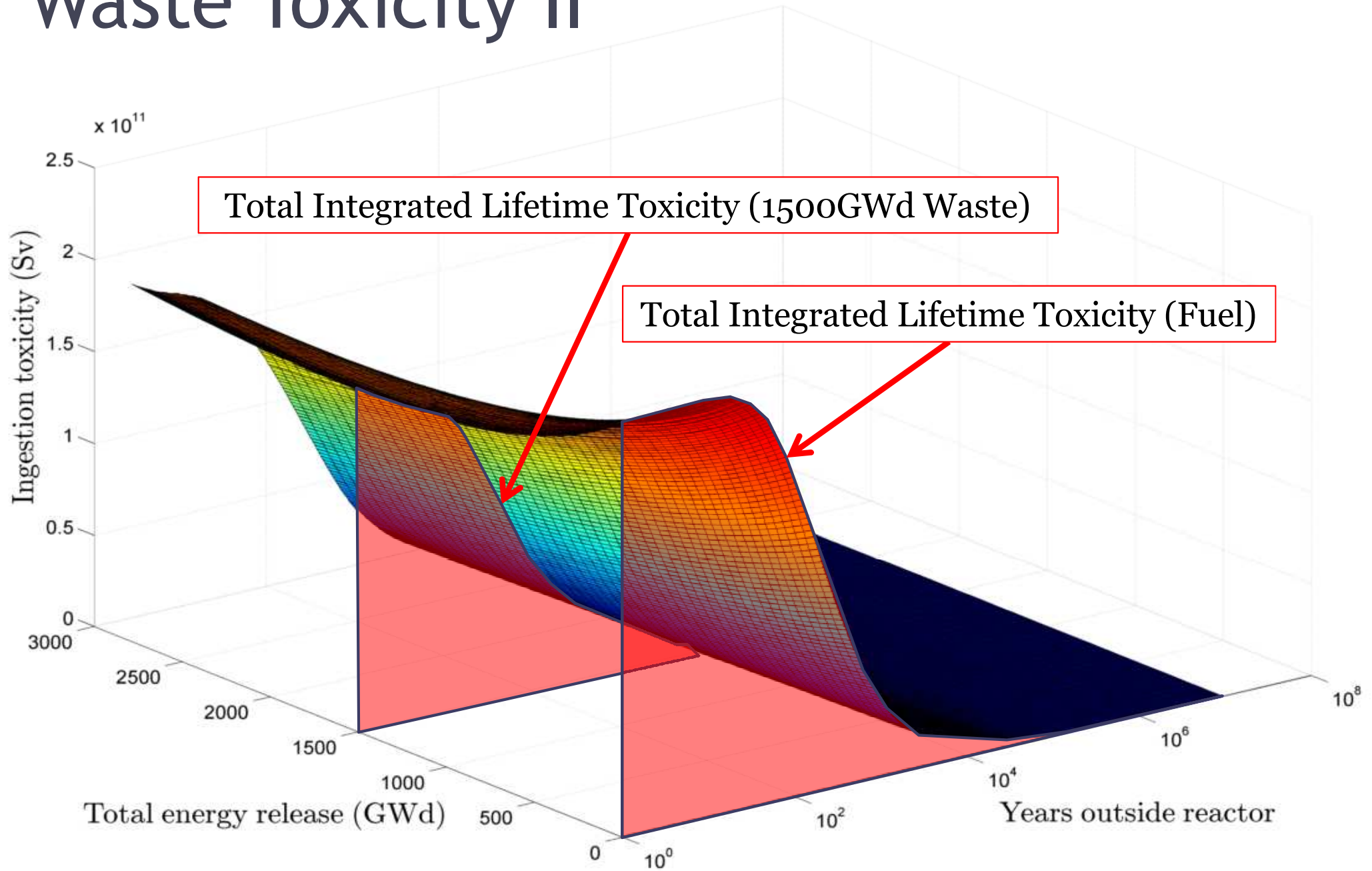
Waste Toxicity II



Waste Toxicity II



Waste Toxicity II



Proliferation Hardness

- Method makes use of Bathke's FOM_1 :

$$FOM_1 = 1 - \log_{10} \left(\frac{M}{800} + \frac{Mh}{4500} + \frac{M}{50} \left[\frac{D}{500} \right]^{\frac{1}{\log_{10} 2}} \right)$$

- 100 years of decay modelled
- Critical mass calculated using diffusion method
- Allows “first-glance” assessment of weapon viability
- Metrics:
 - Worst-case FOM_1
 - Maximum reduction in FOM_1

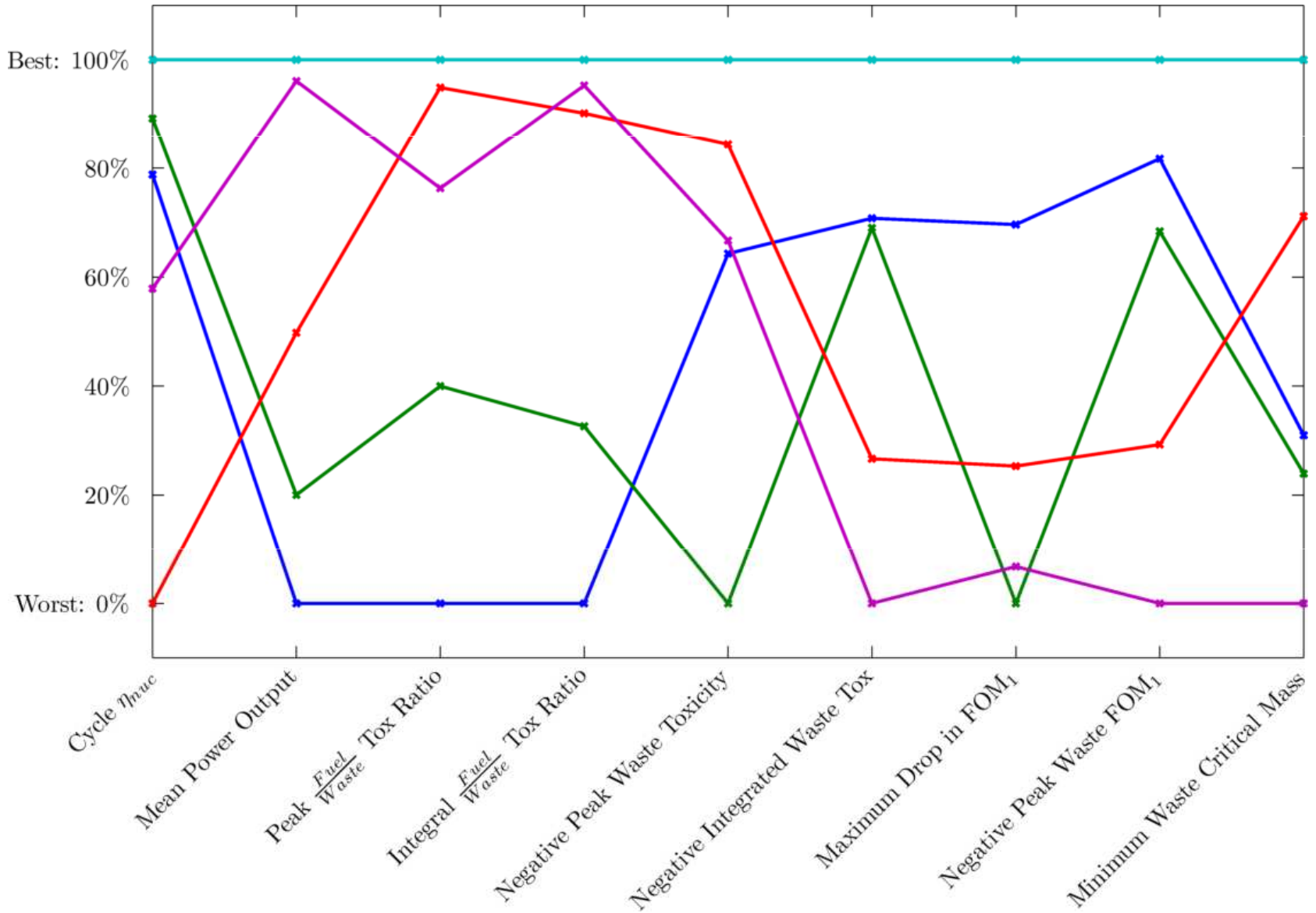
Final Metrics

- Cycle efficiency
- Mean power output
- Ratio of fuel/waste “peak toxicity”
- Ratio of fuel/waste “lifetime toxicity”
- Peak waste toxicity (negative)
- Integrated waste toxicity (negative)
- Maximum reduction in weapon viability
- Peak weapon viability (negative)
- Minimum waste critical mass

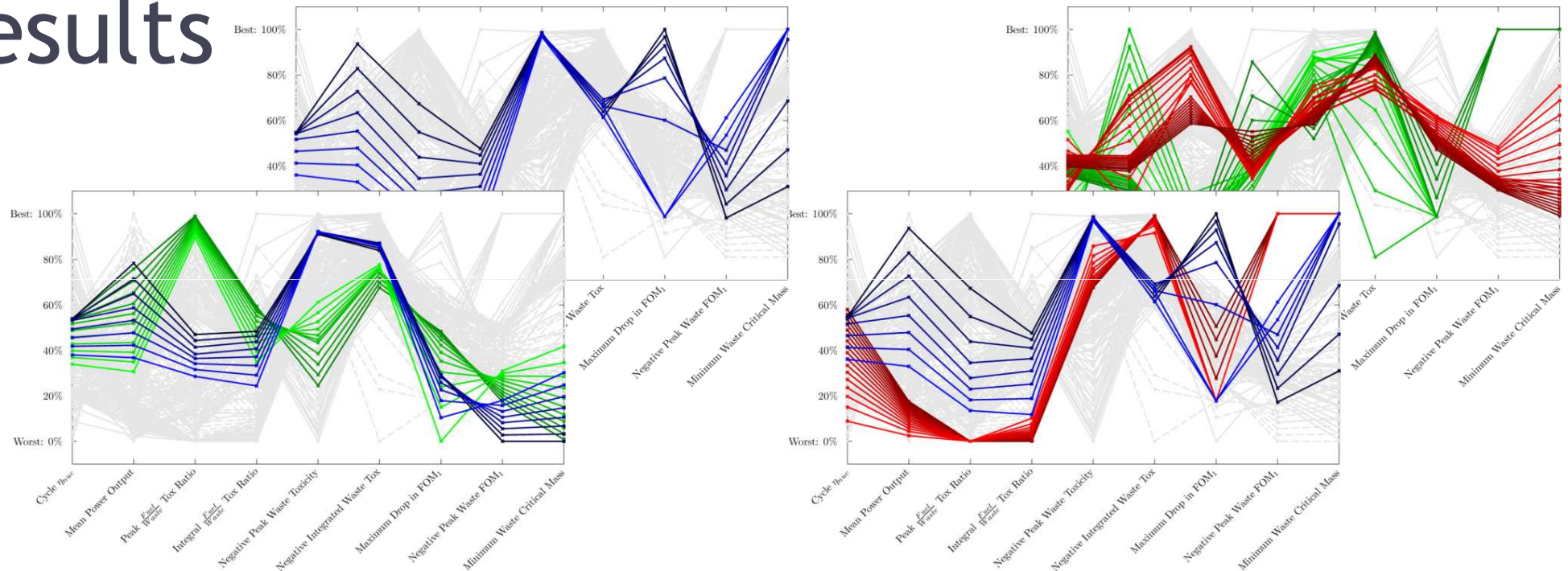
Modelled Cycles

- 4-batch thermal cycles:
 - Enriched uranium (2-10% ^{235}U)
 - Irradiated thorium (2-8% ^{233}U)
 - 5-100% MOx with enriched uranium (3% ^{235}U)
 - 5-100% MOx with irradiated thorium (5% ^{233}U)
- Multi-tier cycles utilising thermal waste
- Fast cycles:
 - Irradiated thorium (6-20% ^{233}U)
 - Superphénix fuel ($^{238}\text{U}/^{232}\text{Th}$, 10-30% Pu)
- Cycles vetted to ensure reasonable reactivity levels
- Both reprocessed and weapons-grade Pu assessed

Results Formatting

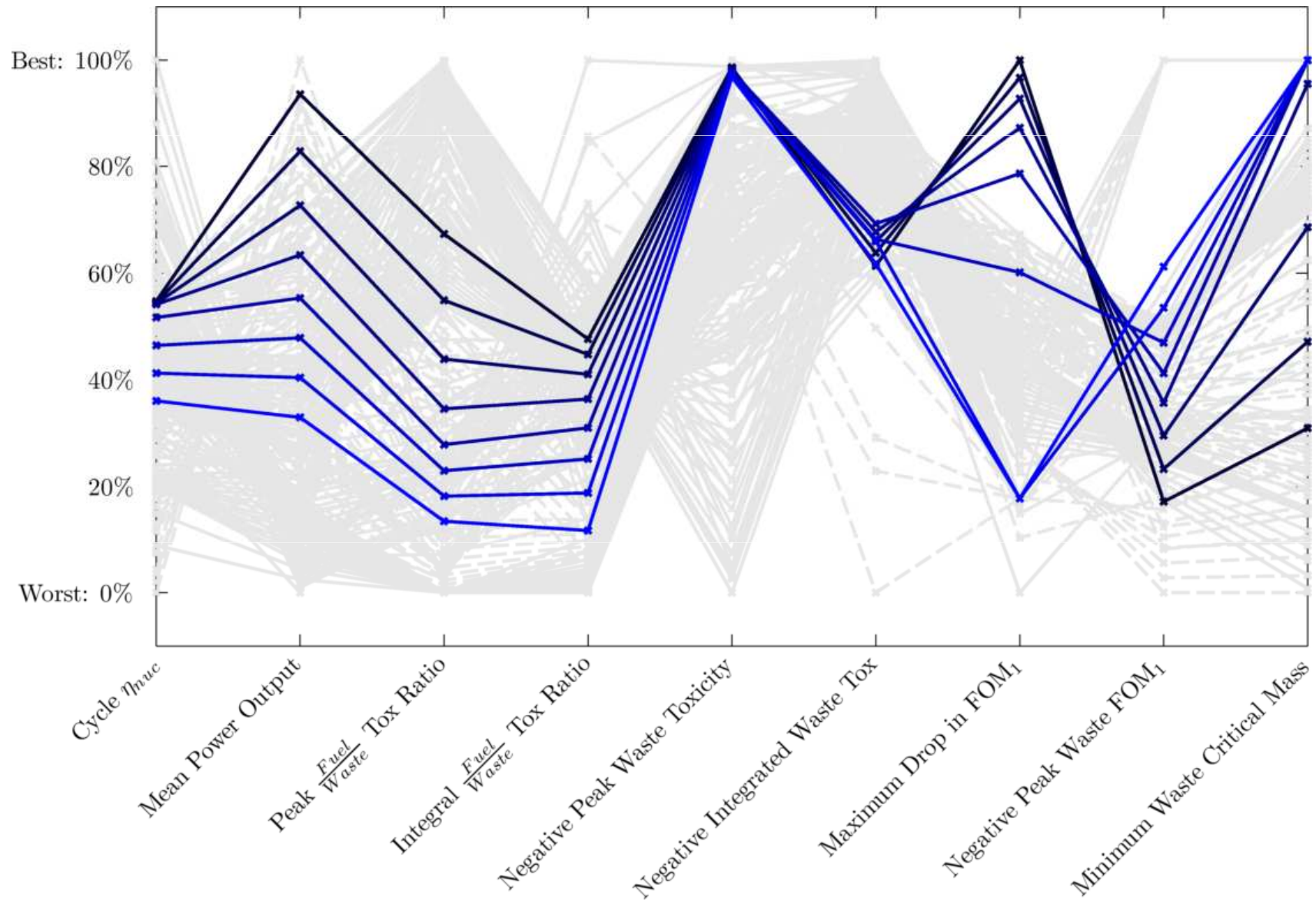


Results

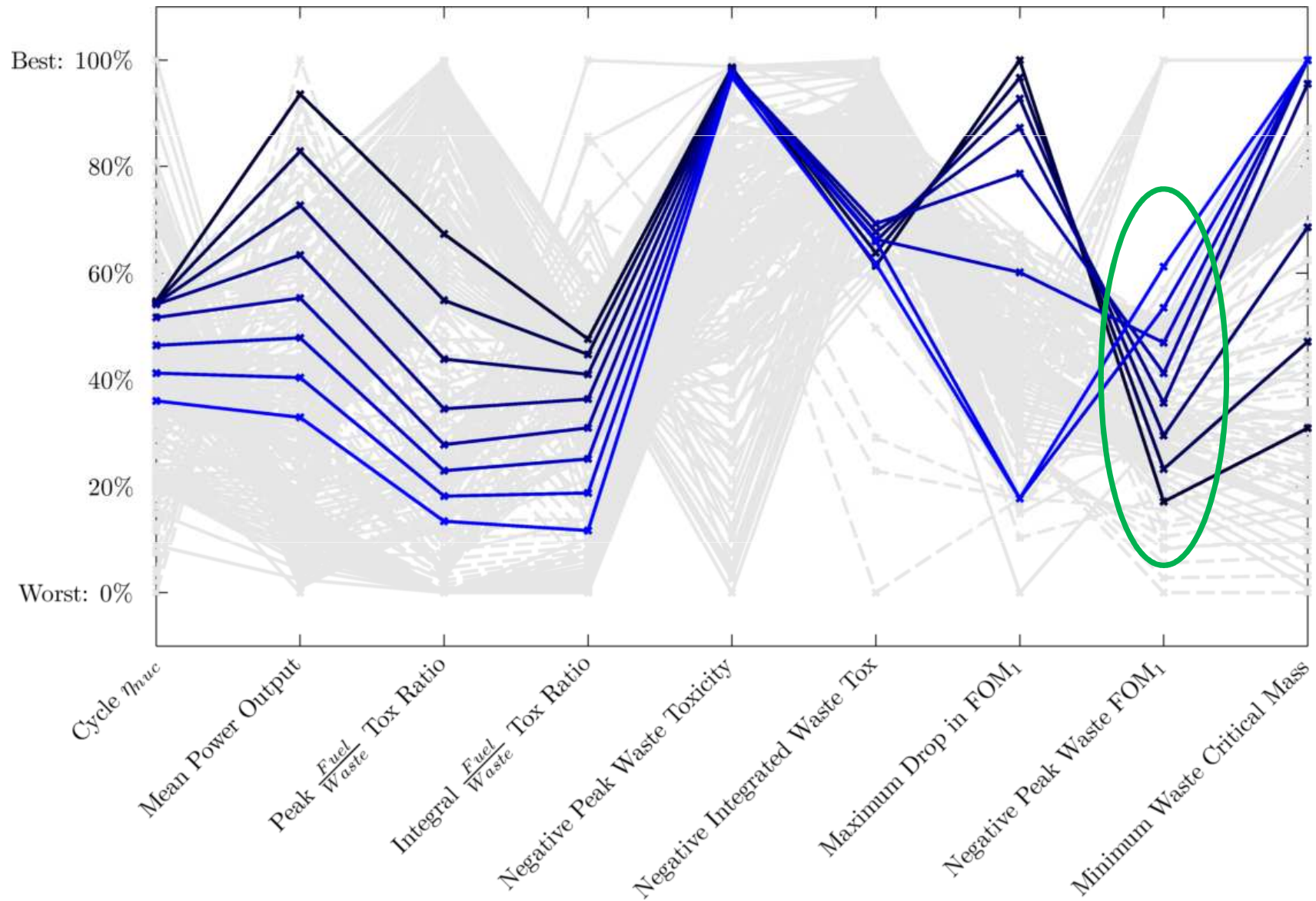


- Cycles can be compared through parallel co-ordinate plots for any or all evaluated metrics
- Some values are truncated, e.g. critical mass
- This allows useful direct comparison between disparate cycles

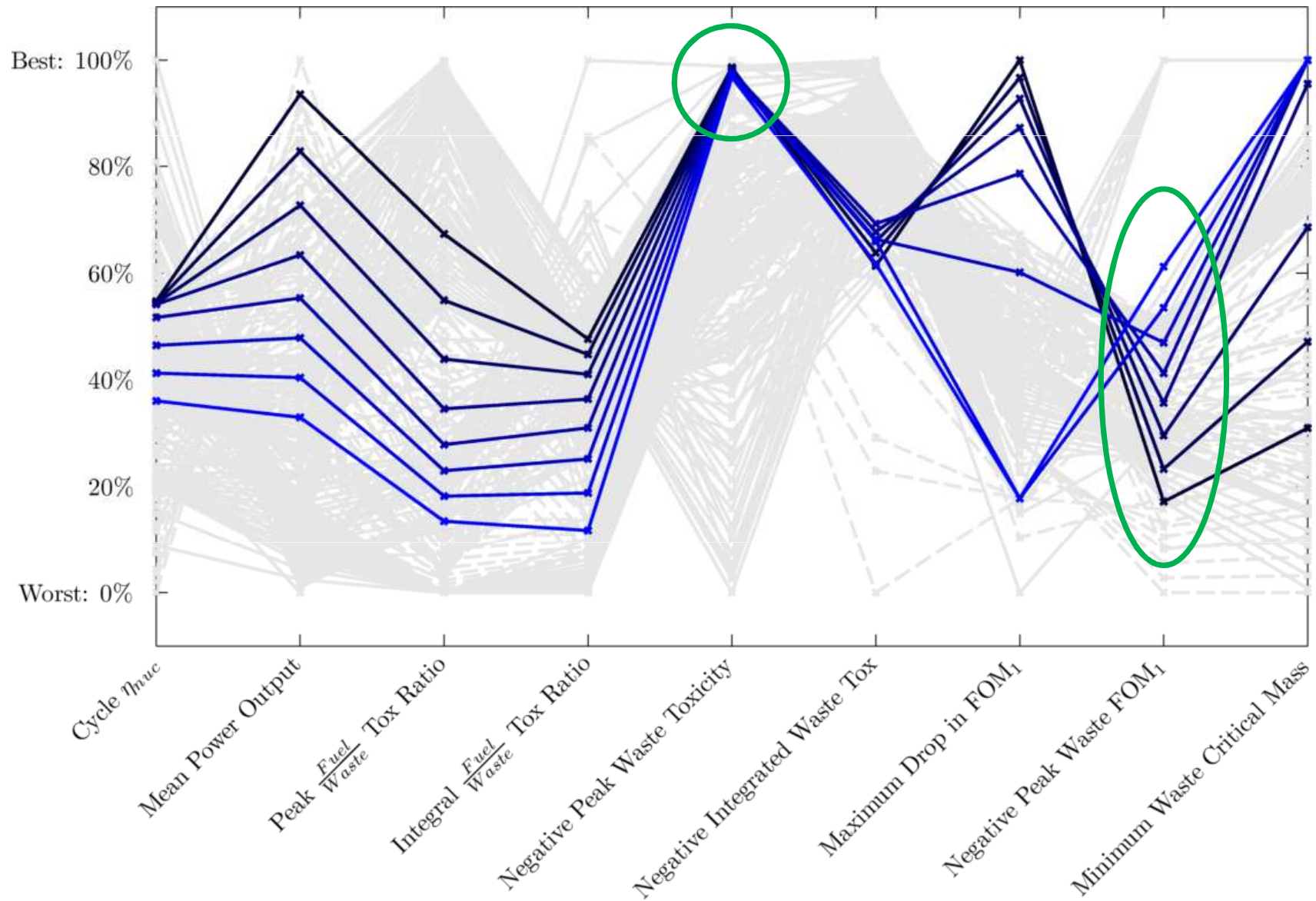
Thorium Fast Cycles



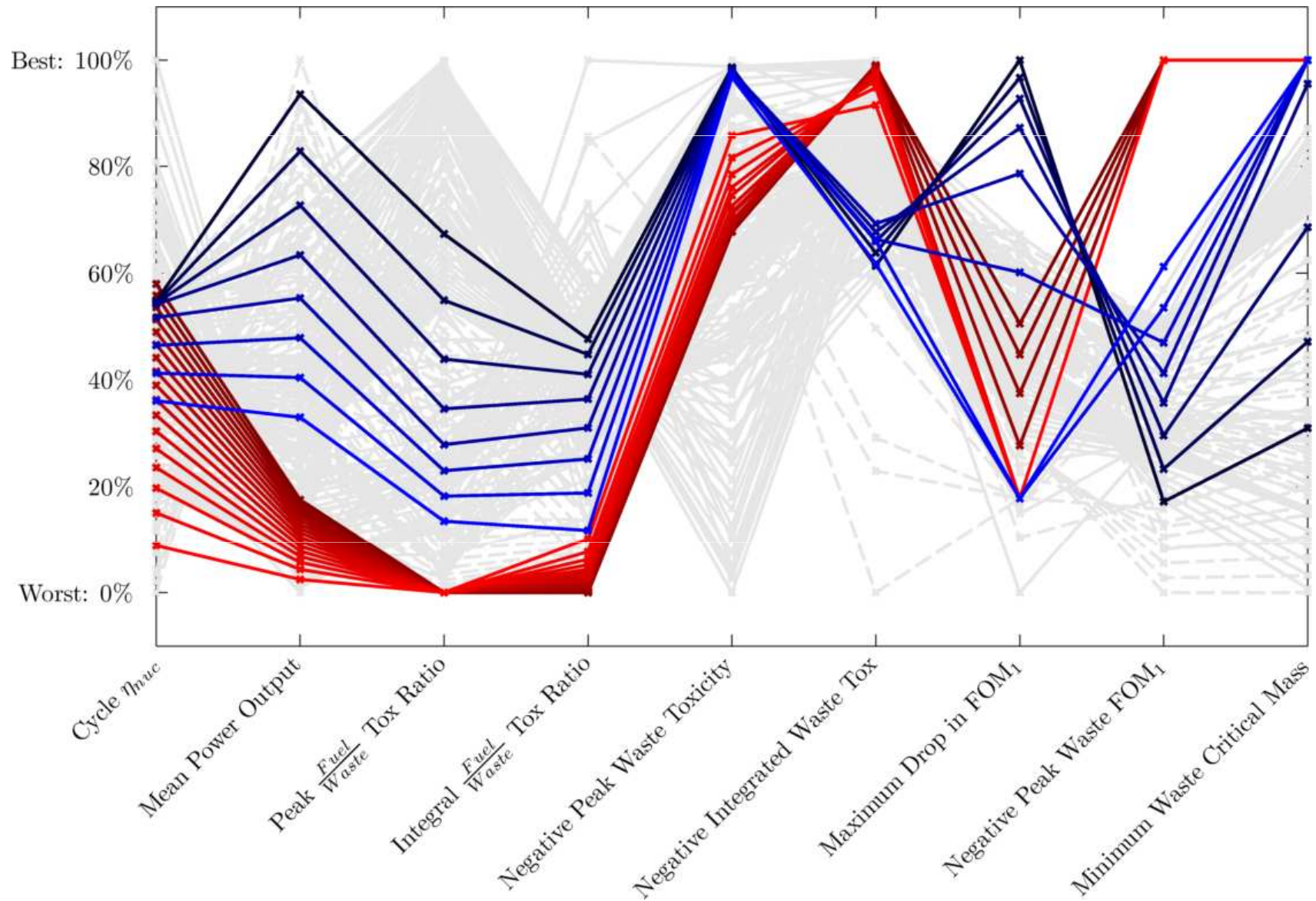
Thorium Fast Cycles



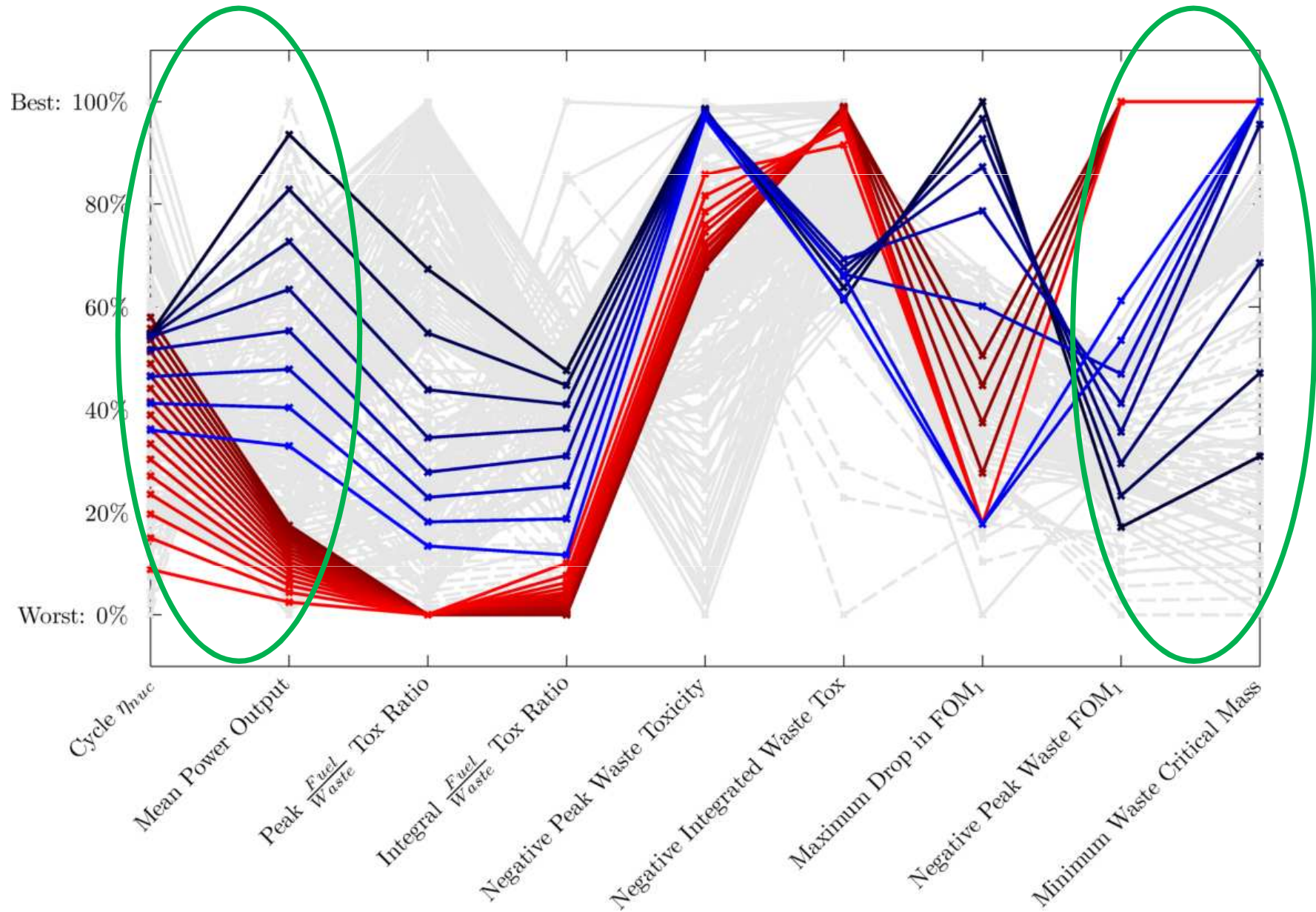
Thorium Fast Cycles



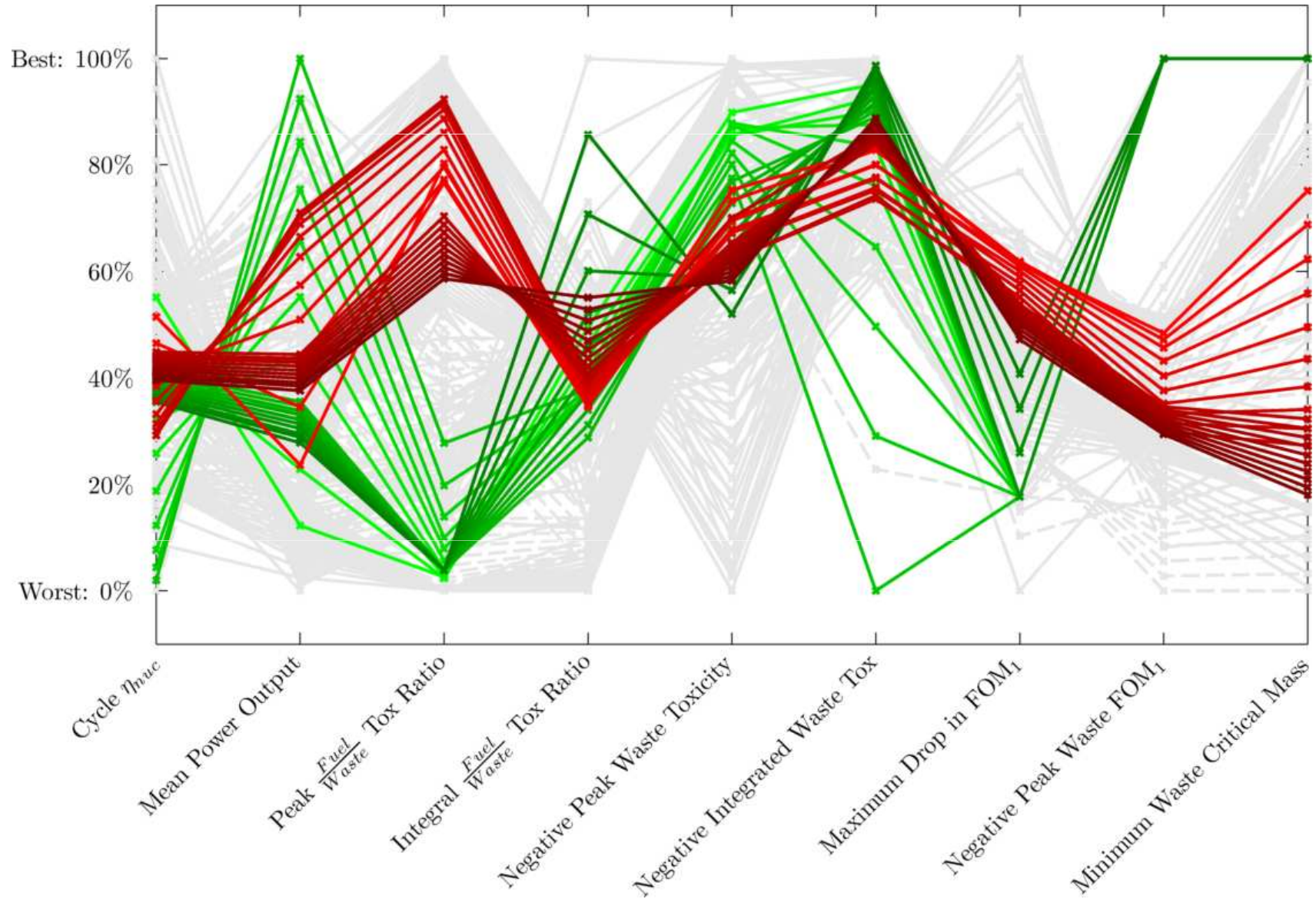
Fast Thorium v. Thermal Uranium



Fast Thorium v. Thermal Uranium



Single v. Multi-Tier



Conclusions I

	Thermal Base								Fast				
	Enriched Uranium	Uranium Multi-Tier	Irradiated Thorium	Thorium Multi-Tier	MOx: Uranium/Pu _D	MOx: Thorium/Pu _D	MOx: Uranium/Pu _w	MOx: Thorium/Pu _w	Irradiated Thorium	Uranium/Pu _D	Thorium/Pu _D	Uranium/Pu _w	Thorium/Pu _w
Efficiency η	●	●	●	●	●	●	●	●	●	●	●	●	●
Power Output	●	●	●	●	●	●	●	●	●	●	●	●	●
Peak Tox. Ratio	●	●	●	●	●	●	●	●	●	●	●	●	●
Tox. Burden Ratio	●	●	●	●	●	●	●	●	●	●	●	●	●
Waste Peak Toxicity	●	●	●	●	●	●	●	●	●	●	●	●	●
Waste Tox. Burden	●	●	●	●	●	●	●	●	●	●	●	●	●
Drop in FOM ₁	●	●	●	●	●	●	●	●	●	●	●	●	●
Waste FOM ₁	●	●	●	●	●	●	●	●	●	●	●	●	●
Critical Mass	●	●	●	●	●	●	●	●	●	●	●	●	●

Conclusions II

- No single dominant cycle
- Almost any comparison possible:
 - Reprocessed vs. weapons-grade Pu
 - Uranium vs. Thorium MOx
 - Fast vs. Thermal
- Methodology allows rapid comparison of fuel cycles
- Could be combined with search optimisation methods to produce optimised cycles

